Understanding Roots

1. Complete the following problem by filling in the blanks for the exponents. Note that a blank may contain a "1" to indicate the first power. Rewrite the problem so that the exponents can be read easily.

$$\sqrt[4]{x^4 y^9 w^3} = x^7 y^7 \sqrt[4]{y^7 w^7}$$

2. Simplify the following roots.

a.
$$\sqrt[3]{18x^8y^3}$$

b.
$$\sqrt{64 x^5 y^9}$$

c.
$$\sqrt[4]{8 x^5 y^{12} z^2}$$

3. Someone in class sort of remembers a rule that "you can't take a root of a negative number." Is this always true, sometimes true or never true? Justify your answer with an explanation.

- 4. Your instructor tells you that there are actually *two* numbers that are the square root of 9. Assuming you believe her...
 - a. What are they?
 - b. Do all numbers have two roots? Are there ever more? (Consider both different numbers and different roots.)